|  |  |
| --- | --- |
| Faculty of Computer & Information Sciences  Ain Shams University  Subject: Math 4  Year: (2nd ) undergraduate  Academic year: 2nd term 2019-2020 |  |

**Research Topic (3)**

**Title: Constant-Harvest Model**

**Introduction about Ordinary differential equation (**Ref. 1**)**

An ordinary differential equation (ODE) is an equation that involves some ordinary derivatives (as opposed to partial derivatives) of a function. Often, our goal is to *solve* an ODE, i.e., determine what function or functions satisfy the equation.

If you know what the derivative of a function is, how can you find the function itself? You need to find the antiderivative, i.e., you need to integrate. For example, if you are given

dx/dt(t)=cost (t)

then what is the function x(t)? Since the antiderivative of cos t is sin t, then x(t) must be sin t. Except we forgot one important point: there is always an arbitrary constant that we cannot determine if we only know the derivative. Therefore, all we can detetermine from the above equation is that

x(t) = sin t + C

for some arbitrary constant C. You can verify that indeed x(t) satisfies the equation dx/dt=cos t.

In general, solving an ODE is more complicated than simple integration. Even so, the basic principle is always integration, as we need to go from derivative to function. Usually, the difficult part is determining what integration we need to do.

**List essential equations to solve initial value problem using Laplace transform** (Ref. 2)

|  |  |
| --- | --- |
| **f(t)={F(s)}** | **F(s)=L{f(t)}** |
| * 1 |  |
|  |  |
| * ,n=1,2,3,… |  |
|  |  |
|  |  |
| * , n=1,2,3,… |  |
| * sin(at) |  |
| * cos(at) |  |
| * tsin(at) |  |
| * tcos(at) |  |
| * sin(at)−atcos(at) |  |
| * sin(at)+atcos(at) |  |
| * cos(at)−atsin(at) |  |
| * cos(at)+atsin(at) |  |
| * sin(at+b) |  |
| * cos(at+b) |  |
| * sinh(at) |  |
| * cosh(at) |  |
| * sin(bt) |  |
| * cos(bt) |  |
| * sinh(bt) |  |
| * cosh(bt) |  |
|  |  |
| * (ct) |  |
| * uc(t)=u(t−c) |  |
| * δ(t−c) |  |
| * uc(t) f(t−c) |  |
| * uc(t) g(t) | L { g(t+c) } |
|  | F(s−c) |
|  |  |
|  |  |
|  |  |
|  | F(s) G(s) |
| * (t+T) = (t) |  |
|  | S F(s) − (0) |
| * ′′(t) | (0)- |
| * (t) | (0)-(0)-(0) |

**Discuss the constant –Harvest Model an explain the meaning of each term in the equation.**

P(t) :the population of fishery

P0 : the initial population

h :harvest rate (decreases the population)

K : growth rate

dp/dt : rate of change of population with time

**Solve the Constant-Harvest Model, Solve the DE subject to P(0) =P0**

**Reference:**

[1] ……………………………………………………………………………

[2] ……………………………………………………………………………

[3] ……………………………………………………………………………

[4] ……………………………………………………………………………

[5] ……………………………………………………………………………

[at least 5 references]